

**Goals** You get a deeper knowledge of Burstall's memory model.

### Exercise 1 [4] Heap Basics

1. What is the meaning of  $p$ ,  $q$ , and  $xs$  in the abstraction predicate `list node-alloc node-next p xs q` for lists?
2. What is the purpose of the parameters `node-alloc` and `node-next`?
3. For every abstraction predicate, we need a separation lemma. What is its purpose? (Look at examples and then give a general explanation)
4. Why can Burstall's memory model not be used for arbitrary C programs? Give an example for a program, which is not correctly modeled.

### Exercise 2 [6] Sum of List Elements

(a) [5] The following code iterates through a list at  $p$  and computes the sum of all elements

```
s = 0;
while (p != null) {
  s = s + p->data;
  p = p->next;
}
```

The precondition requires that the list is allocated and binds the auxiliary variable  $P$ .

`list node-alloc node-next p XS NULL  $\wedge$  p = P`

The postcondition ensures that the result  $s$  is really the sum of the data fields of the list elements.

`s = listsum (list-data node-data XS)`

The invariant is similar to `list_length` from the lecture, but we need to consider the part of the list we already visited, too.

$\exists ys zs.$   
`list node-alloc node-next P ys p  $\wedge$`   
`list node-alloc node-next p zs NULL  $\wedge$`   
`XS = ys @ zs  $\wedge$`   
`s = listsum (list-data node-data ys)`

Your task is to do a detailed proof to understand which lemmas are required at which point.

(b) [1] Try to find a proof which is as automatic as possible. For this, extend the current `simpset` step-by-step by using

`declare ... [simp]`

instead of passing the theorems to every `simp` call.

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