

Homework 1 (Normal Forms)

Recall the inductive definition of the set NF of *normal forms*:

$$\frac{\frac{t \in \text{NF}}{\lambda x. t \in \text{NF}} \quad n \geq 0 \quad t_1 \in \text{NF} \quad t_2 \in \text{NF} \quad \dots \quad t_n \in \text{NF}}{x t_1 t_2 \dots t_n \in \text{NF}}$$

Show that this set precisely captures all normal forms, i.e.:

$$t \in \text{NF} \Leftrightarrow \nexists t'. t \rightarrow_\beta t'$$

Homework 2 (Weakly Normalising Terms)

Inductively define the set of weakly normalising terms WN, i.e. the set of terms that have a β -normal form. In particular it should hold that

$$s \in \text{WN} \iff \exists t. s \Rightarrow_n t.$$

Similarly, define the set of strongly normalising terms SN where a term s is strongly normalising if there is no infinite sequence $\{t_i. i \in \mathbb{N}\}$ with $s \rightarrow_\beta^* t_0$ and $t_i \rightarrow_\beta t_{i+1}$ for $i \in \mathbb{N}$.

Give a term t that is weakly but not strongly normalising.